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1. (12 points) This problem concerns the function $f(x)=60 x-9 x^{2}-2 x^{3}$.
(a) Find the critical points.
(b) Find the intervals on which $f$ increases and on which it decreases.
(c) Use your answer from part (a) to identify the locations ( $x$ values) of any local extrema of $f$.
2. (8 points) The graph of the derivative $f^{\prime}(x)$ of a function $f(x)$ is shown below.
(a) State the critical points of $f$.
(b) State the interval(s) on which $f$ increases.
(c) State the interval(s) on which $f$ decreases.
(d) Using the same coordinate axes, sketch a
 possible graph of $y=f(x)$.
Be sure to clearly indicate any local extrema.
3. (12 points) This problem concerns the function $f(x)=x^{2} e^{x}-3 e^{x}$.
(a) Find the critical points.
(b) Find the intervals on which $f$ increases and on which it decreases.
(c) Use your answer from part (a) to identify the locations ( $x$ values) of any local extrema of $f$.
4. (8 points) The graph of the derivative $f^{\prime}(x)$ of a function $f(x)$ is shown below.
(a) State the critical points of $f$.
(b) State the interval(s) on which $f$ increases.
(c) State the interval(s) on which $f$ decreases.
(d) Using the same coordinate axes, sketch a
 possible graph of $y=f(x)$.
Be sure to clearly indicate any local extrema.
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5. (12 points) This problem concerns the function $f(x)=\ln \left(x^{2}-6 x+10\right)$.
(a) Find the critical points.
(b) Find the intervals on which $f$ increases and on which it decreases.
(c) Use your answer from part (a) to identify the locations ( $x$ values) of any local extrema of $f$.
6. (8 points) The graph of the derivative $f^{\prime}(x)$ of a function $f(x)$ is shown below.
(a) State the critical points of $f$.
(b) State the interval(s) on which $f$ increases.
(c) State the interval(s) on which $f$ decreases.
(d) Using the same coordinate axes, sketch a
 possible graph of $y=f(x)$.
Be sure to clearly indicate any local extrema.
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7. (12 points) This problem concerns the function $f(x)=3 x^{4}+4 x^{3}-2$.
(a) Find the critical points.
(b) Find the intervals on which $f$ increases and on which it decreases.
(c) Use your answer from part (a) to identify the locations ( $x$ values) of any local extrema of $f$.
8. (8 points) The graph of the derivative $f^{\prime}(x)$ of a function $f(x)$ is shown below.
(a) State the critical points of $f$.
(b) State the interval(s) on which $f$ increases.
(c) State the interval(s) on which $f$ decreases.
(d) Using the same coordinate axes, sketch a
 possible graph of $y=f(x)$.
Be sure to clearly indicate any local extrema.
