

Directions: Please answer in the space provided. No calculators. Please put all phones, etc., away.

1. Suppose T is a linear transformation defined as $T(\mathbf{x}) = A\mathbf{x}$, where $A = \begin{bmatrix} 5 & -3 \\ 1 & 1 \\ 1 & -1 \end{bmatrix}$.

(a) State the domain of T .

(b) State the codomain of T .

(c) Find the kernel of T .

(d) Find the range of T .

(e) $\text{nullity}(T) =$

(f) $\text{rank}(T) =$

(g) Is T one-to-one?

(h) Is T onto?

2. Suppose $S : P_2 \rightarrow P_2$ is a linear transformation for which $S(1) = x - x^2$, $S(x) = 1 + x + 3x^2$ and $S(x^2) = 4$.

Find $S(3 - x + 2x^2)$.