

- 8 An object moving on a straight line is $s(x) = \frac{x}{x^2+1}$ feet from its starting point at time x . What is its acceleration when its velocity is 0 ft/sec?

$$\text{Velocity} = v(x) = s'(x) = \frac{1 \cdot (x^2+1) - x \cdot 2x}{(x^2+1)^2} = \frac{1+x^2}{(x^2+1)^2}$$

$$= \frac{(1-x)(1+x)}{(x^2+1)^2}$$

Thus the velocity is 0 at

times $x=1$ and $x=-1$ seconds. Since we're assuming time is not negative, the velocity is 0 at time $x=1$

Now, acceleration is $v'(x) = \frac{-2x(x^2+1)^2 - (1-x^2)2(x^2+1)2x}{(x^2+1)^4}$

$$= \frac{-2x(x^2+1) - 4x(1-x^2)}{(x^2+1)^3}$$

Acceleration at time $x=1$ is $v'(1) = \frac{-2(1^2+1) - 4(1-1^2)}{(1+1)^3} = \boxed{-1 \text{ ft/sec}^2}$

- 22 $f(x) =$ (# of liters of fuel when rocket is x miles high)
 $f'(x) =$ rate of change of liters of fuel, in liters/mile.

$f'(20) = -8$ means when rocket is 20 miles is high it is using fuel at a rate of 8 liters per mile. In going from 20 to 21 miles high, expect to use 8 liters of fuel.