

# Chapter 12

MATH 200

$$\textcircled{2} \lim_{x \rightarrow 3^+} \frac{x^2 - x}{x^2 - 9} = \boxed{\infty}$$

← approaching  $3^2 - 3 = 6$   
← approaching 0, positive

$$\textcircled{4} \lim_{x \rightarrow 1^+} \ln\left(\frac{x^2 - x}{x - 1}\right) = \lim_{x \rightarrow 1^+} \ln\left(\frac{x(x-1)}{x-1}\right)$$
$$= \lim_{x \rightarrow 1^+} \ln(x) = \ln(1) = \boxed{0}$$

$$\textcircled{6} \lim_{x \rightarrow \pi^+} \frac{\cos(x)}{1 + \cos(x)} = \boxed{-\infty}$$

← approaches -1  
← approaches 0, positive

$$\textcircled{8} \lim_{x \rightarrow 0^+} \frac{\sin(x)}{x^2} = \lim_{x \rightarrow 0^+} \underbrace{\frac{\sin(x)}{x}}_{\text{approaches 1}} \cdot \underbrace{\frac{1}{x}}_{\text{approaches } \infty} = \boxed{\infty}$$

18 Find the vertical asymptotes of  $f(x) = \frac{15 - 12x - 3x^2}{50 - 2x^2}$

$$f(x) = \frac{3(5 - 4x - x^2)}{2(25 - x^2)} = \frac{3(5+x)(1-x)}{2(5-x)(5+x)} = \frac{3(1-x)}{2(5-x)} \quad \text{For } x \neq -5$$

Denominator is 0 for  $x = 5$  and  $x = -5$ , so these are the candidates for the vertical asymptotes.

Check  $x = 5$   $\lim_{x \rightarrow 5^+} f(x) = \lim_{x \rightarrow 5^+} \frac{3(1-x)}{2(5-x)} = \boxed{\infty}$

Check  $x = -5$   $\lim_{x \rightarrow -5} f(x) = \lim_{x \rightarrow -5} \frac{3(1-x)}{2(5-x)} = \frac{18}{20} = \frac{9}{10} \neq \infty$

ANS The line  $x = 5$  is the only vertical asymptote