Density Functional Theory Study of the Interaction of Hydrogen with Li$_6$C$_{60}$

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ABSTRACT: Hydrogen storage properties of Li-coated C$_{60}$ fullerene have been studied using density functional theory within the local density as well as generalized gradient approximation. Hydrogen atoms are found to bind to Li$_6$C$_{60}$ in two distinct forms, with the first set attaching to C atoms, not linked to Li, in atomic form. Once all such C atoms are saturated with hydrogen, the second set of hydrogen atoms bind quasi-molecularly to the Li atoms, five of which remain in the exohedral and the sixth in the endohedral position. The corresponding hydrogen gravimetric density in Li$_6$C$_{60}$H$_{40}$ is 5 wt %. Desorption of hydrogen takes place in succession, the ones bound quasi-molecularly desorbing at a temperature lower than the ones bound atomically. The results are compared with the recent experiment on hydrogen adsorption in Li$_6$C$_{60}$.

SECTION: Energy Conversion and Storage; Energy and Charge Transport

Ideal hydrogen storage materials for mobile applications require the host material to be light and to operate at near-ambient thermodynamic conditions. For the latter requirement, hydrogen binding should be intermediate between physisorption and chemisorption. Unfortunately, lightweight materials such as Li and C bind hydrogen strongly. For example, in LiH, hydrogen desorbs at 670 °C, while in hydrogenated C$_{60}$ fullerene, C$_{60}$H$_x$ (often referred to as fulleranes or hydrofullerenes), hydrogen desorbs at temperatures above 500 °C. In addition, the fulleranes release hydrocarbons during hydrogen desorption, thus making fulleranes unsuitable for reversible hydrogen storage. It was suggested that one can avoid this problem by doping C$_{60}$ with Li. Because C$_{60}$ has a large electron affinity, charge transfer from Li to C$_{60}$ cage makes Li positively charged, and the electric field produced by such point charges can bind hydrogen through the polarization mechanism. In such a case, H$_2$ molecules are polarized and bind to Li in quasi-molecular form with a binding energy lying between physisorption and chemisorption. This makes it possible for hydrogen to desorb at near-ambient conditions. It was predicted that Li$_{12}$C$_{60}$ can reversibly store as much as 13 wt % hydrogen in quasi-molecular form.

Recently Teprovich et al. have carried out an experiment using solvent-assisted mixing in which the molar ratio of LiH/C$_{60}$ was varied from 120:1 to 2:1. The authors found that Li$_x$C$_{60}$ was capable of storing hydrogen reversibly through chemisorption at elevated temperatures and pressures. In particular, Li$_6$C$_{60}$ with a molar ratio of 6:1 can reversibly desorb up to 5 wt % H$_2$ with an onset temperature of ~270 °C. In addition, the fullerene cage remained mostly intact and was only slightly modified during the desorption/adsorption cycle. Furthermore, no release of hydrocarbons was noticed. These exciting results, however, leave some fundamental questions unanswered. (1) For example, where do Li atoms reside in C$_{60}$? Do they occupy an exohedral or endohedral position? Do they cluster or remain isolated? (2) As Li doped C$_{60}$ is hydrogenated, where do the hydrogen atoms reside? Do they bind to Li or C atoms and in what form? (3) What is the maximum number of H atoms that can bind to the Li$_6$C$_{60}$ surface and does their binding energy depend upon the amount of hydrogen adsorbed? (4) Why does the Li$_6$C$_{60}$ cage not break up and release hydrocarbons while the C$_{60}$ fullerene does during dehydrogenation? (5) Why does hydrogen desorb at a much lower temperature in hydrogenated Li$_6$C$_{60}$ than in fulleranes? In this Letter, we provide answers to some of these questions by carrying out detailed density functional theory based calculations. In the following, we give a brief description of our theoretical procedure, which is followed by a discussion of our results and a summary of our conclusions.

Site preference of Li and H atoms on C$_{60}$, the total energies of Li-decorated C$_{60}$ with and without hydrogen loading, and the electronic structure of Li$_x$C$_{60}$H$_x$ were calculated using density functional theory and the Perdew–Burke–Ernzerhof (PBE) form for the generalized gradient-corrected (GGA) exchange–correlation functional. We used a plane wave basis set and the projector augmented wave method as implemented in the Vienna ab initio Simulation Package (VASP). The supercell approach was used where clusters were placed at the center of a 24 × 24 × 24 Å$^3$ cubic cell. Due to the large supercell, the Brillouin zone integration was performed only at the Γ point. The energy cutoff was set at 400 eV. In all calculations, self-
consistency was achieved with a tolerance in the total energy of at least 0.01 meV. Hellman–Feynman force components on each ion in the supercells were converged to 1 meV/Å. The structures were optimized without any symmetry constraint. In the case of hydrogen molecules binding weakly to the Li metal ions, calculations were repeated using local density approximation (LDA). This is because DFT does not treat dispersive forces properly and GGA is known to cause underbinding. On the other hand, LDA leads to overbinding and somehow compensates for the lack of dispersive forces in DFT. Test calculations have shown that binding energies in weakly coupled systems computed using LDA are in better agreement with those from experiment as well with those based on second-order Moller–Plesset perturbation theory (MP2) and the coupled cluster method with singles and doubles and noniterative inclusion of triples [CCSD(T)]. We have also performed IR stability calculations to ensure that the geometries presented in this Letter are dynamically stable and contain no imaginary frequencies.

**Site Preference of Li As a Function of Li Concentration.** We first discuss the geometry of Li,C60 (x = 1, 6). To determine the preferred site of Li on C60, we first calculated the total energies of Li,C60 by placing the Li atom on the five-fold and six-fold hollow sites. The preferred site is one where Li binds to the five-fold site, while the one bound to the six-fold site is 60 meV higher in energy. This is in agreement with earlier calculations.

The energy barrier when the Li atom moves from the pentagon to the hexagon site across a C–C bridge was calculated to be 0.35 eV by using the nudged elastic band (NEB) method implemented in VASP code. This barrier is larger than the 0.2 eV barrier in the (5,5) carbon nanotube when a Li atom moves across a C–C bridge from one hexagon to another along the nonaxial direction. Although C60 and the (5,5) carbon nanotube have very similar diameters, the pentagon to hexagon migration in C60 results in a larger energy barrier. Because this is much larger than the thermal energy corresponding to the room temperature, Li migration is unlikely under ambient thermodynamic conditions.

There are many possibilities for the geometry of Li,C60. Here, Li atoms may occupy near-neighbor sites, remain isolated from each other, or form either endohedral or exohedral complexes. In Figure 1, we provide the optimized geometry of four low-lying isomers of Li,C60 with Li atoms having the freedom to occupy an exohedral or endoheral position as well as forming isolated or clustered configurations. The configuration with Li atoms bound to exohedral sites and occupying near-neighbor positions has the lowest energy, but the other geometries are energetically nearly degenerate. This is because there is virtually no interaction between the Li atoms because the Li–Li binding energy (1.10 eV) is much smaller than the Li–C binding energy (2.83 eV). In addition, the binding energy per Li atom in Li,C60 defined as

$$E_x(Li) = -\frac{[E(Li_xC_{60}) - E(C_{60}) - xE(Li)]}{x}$$

is 1.53 eV for x = 1 and 1.76 eV for x = 6. The small difference in E_x(Li) suggests that Li atoms may randomly occupy five-fold sites in C60. IR stability calculations confirmed the dynamical stability of the geometries with no imaginary frequencies. In Figure 2, we plot the highest occupied molecular orbital (HOMO) and the lowest unoccupied molecular orbital (LUMO) corresponding to the lowest-energy structure in Figure 1(a1). We find that the C atoms in the two adjoining pentagons along the C_x axis contribute more to the HOMO than to the LUMO, as shown in Figure 2(a1) and (a2), respectively.

**Site Preference of H As a Function of Li Concentration (Li_xC_{60}H_y).** Using total energy calculations, we first determine the preferred site of one H atom in Li,C60 by placing it atop the Li site. Next, we considered H atop the C atom nearest to the Li atom as well as the C site farthest from the Li atom. Again, the geometries are fully relaxed for each configuration. The resulting optimized geometries and relative energies measured with respect to the lowest-energy configuration are given in Figure 3. We note that the clearly preferred configuration for the H atom is where it attaches to the on-top C site that is nearest to the Li atom (Figure 4b). We define the binding energy of hydrogen as

$$E_b(H) = -\frac{[E(Li_xC_{60}H) - E(Li_xC_{60}) - E(H)\frac{\text{total}}{x}]}{x}$$

Figure 1. Geometries of the ground-state (a1) and low-lying isomers (a2), (b1), and (b2) of Li,C60 clusters. Relative energies $\Delta \varepsilon$ of each cluster with respect to the ground state are also given. The symmetries of (a1), (b1), and (a2) structures are $C_{5v}$ while that of (b2) is $C_2$.

Figure 2. (a1) HOMO and (a2) LUMO of the Li6C60 cluster with $C_{5v}$ symmetry; (b1) HOMO and (b2) LUMO of the lowest-energy configuration of the Li6C60–40H cluster.
This binding energy is 2.76 eV. This needs to be compared with the 3.58 eV binding energy of H to C in a CH dimer and the 2.34 eV binding energy of H to Li in a LiH dimer. This comparison establishes why H prefers to bind to C rather than to Li. To understand why H prefers to bind to a C atom that is nearest to the Li atom rather than to the one farthest removed, we note that H prefers to remain as a \( \text{H}^- \) ion. The charge transfer from Li to C\(_{60} \) puts extra electrons in the vicinity of the Li atom, enabling the C atoms nearest to C\(_{60} \) to donate electrons to H more easily.

We next consider the geometry of Li\(_6\)C\(_{60}\) decorated with 40 H atoms as this corresponds to 5 wt % hydrogen seen experimentally to desorb around 270 °C. The questions that need to be answered are as follows: (1) Where do these H atoms reside? (2) Does the location of the Li atoms on C\(_{60} \) change as more hydrogen atoms are adsorbed? (3) What is the average binding energy of H per atom in Li\(_6\)C\(_{60}\)H\(_x\)? and how does it compare to that in C\(_{60}\)H\(_x\)? (4) Does the C\(_{60} \) cage remain unaffected as Li and H atoms are loaded? To answer these questions, six configurations were considered (see Figure 4).

We first introduced H atoms on top of Li and C atoms in such a way that the 40 H atoms were distributed over the entire C\(_{60} \) surface with H atoms binding to C or Li atoms [Figure 4(a\(_1\))]. Second, we allowed the H atoms to cluster over the C\(_{60} \) surface [Figure 4(a\(_2\))]. In the third configuration [Figure 4(a\(_3\))], some of the H atoms were bound to Li atoms in quasi-molecular form, while others were bound to C atoms chemically. In these three configurations, the Li atoms were kept on exohedral sites. The calculations were repeated by allowing Li atoms to occupy both exohedral and endohedral positions. Three of the low-lying isomers, optimized without any symmetry constraint, are shown in Figure 4(b\(_1\)), (b\(_2\)), and (b\(_3\)). The relative energies measured with respect to the lowest-energy structure are given in Figure 4. Thermodynamically, the most stable structure [Figure 4(b\(_2\))] is the one where five Li atoms remain on the outside, with each binding to one H\(_2\) molecule in quasi-molecular form. The sixth Li atom becomes endohedral and does not bind to any H atom. The other 30 H atoms bind to 30 C atoms not coordinated with Li. The degeneracy between the Li\(_6\)C\(_{60} \) structures with five Li atoms on the outside and one Li atom on the inside versus that with all six Li atoms on the outside (see Figure 1) is lifted once H atoms are adsorbed. Note that the structure where six Li atoms are on the outside binding to five H\(_2\) molecules [Figure 4(a\(_3\))] is 2.53 eV higher in energy than the ground-state structure.

The ground-state structure in Figure 4(b\(_2\)) is interesting. Here, the C atoms linked to Li do not bind H. Because for each Li atom there are five such C atoms, a total of 30 C atoms in C\(_{60} \) cannot bind hydrogen. That leaves only 30 C atoms, each of which binds to one H atom. Because Li atoms are positively charged, they bind hydrogen in quasi-molecular fashion due to the charge polarization mechanism discussed earlier.\(^{13,14}\) Thus, five Li atoms bind five H\(_2\) molecules, and the geometry in Figure 4(b\(_2\)) completely accounts for all of the H atoms attached in Li\(_6\)C\(_{60}\)H\(_{40}\). We also note that the structure of the C\(_{60} \) cage gets distorted as Li and H atoms are bound.

In order to better understand the lowest-energy structure of Li\(_6\)C\(_{60}\)H\(_{40} \) as shown in Figure 4(b\(_2\)), where one Li atom is inside of the cage, we calculated the energy barrier that needs to be overcome by Li for insertion into the cage. One possible scenario is that at high temperature, one Li atom may diffuse...
from one pentagon to the nearest hexagon from which it can enter into the cage. We, therefore, calculated this energy barrier, which was found to be 6.95 eV. While this is very large, it is possible that it is smaller than the penetration energy barrier of 7.40 eV on a graphene sheet.

This can be understood with the following two factors: First, in C_{60}, the longer C–C bond between a hexagon and a pentagon is 1.458 Å, and the shorter C–C bond length between the two hexagons is 1.40 Å. The average C–C bond length in a hexagon is 1.429 Å, which is larger than that (1.40 Å) in the graphene sheet. Second, due to the curvature of the C_{60} surface, the p_{x} orbitals are orientated more outwardly, which would further reduce the energy barrier when the Li atom enters the cage. It is likely that under experimental conditions, all of the Li atoms may reside on the exohedral positions. In that case, the sixth Li atom can also bind to one H_{2} molecule, thus increasing the number of hydrogen atoms from 40 to 42. Note that the exact number of H atoms attached to Li_{6}C_{60} was not determined in the above experiment, and the authors estimated it to be around 40.

**Binding Energy of Hydrogen to C_{60} versus Li_{x}C_{60}**

As mentioned earlier, the binding energy of a H atom to C_{60} decorated with a single Li atom is 2.76 eV. In order to see how this binding energy changes with respect to multiple hydrogen decoration, we first consider the average binding energy of H in the Li_{6}C_{60}H_{30} cluster. Here, H atoms are bound to the 30 C atoms that are not linked to Li. The average H binding energy is defined as

\[
\langle E_{b}(H) \rangle = -\frac{[E(Li_{6}C_{60}H_{30}) - E(Li_{6}C_{60}) - 30E(H)]}{30}
\]

We find \( \langle E_{b}(H) \rangle \) to be 2.64 eV. Because this is rather close to the binding energy of 2.76 eV in Li_{6}C_{60}H, one can conclude that the binding energy of H is not very sensitive to the number of Li atoms that decorate C_{60}. To examine how these binding energies compare with that in pristine C_{60}, we have calculated the optimized structures of C_{60}H_{30} and C_{60}H_{60} clusters. While there is no ambiguity in the structure of C_{60}H_{30} as there is one H atom for every C atom, there are numerous choices for the possible structure of C_{60}H_{60}. We considered an initial geometry for C_{60}H_{30} by removing the six Li atoms and five quasi-molecularly bound H_{2}’s from Figure 4(b). The structure was then reoptimized. The calculated average binding energies of the H atom in the C_{60}H_{30} and C_{60}H_{60} clusters were 2.54 and 2.44 eV, respectively. These energies are slightly smaller than those in Li_{6}C_{60}H_{30} and Li_{6}C_{60}H_{60} respectively. In other words, hydrogen binds more strongly to Li-coated C_{60} than to pristine C_{60}. The question then remains, Why does hydrogen desorb from Li_{6}C_{60}H at a lower temperature than that from C_{60}H_{2}? Thermodynamically this should not be the case because H is bound to C in Li_{6}C_{60}H_{30} at least as strongly as that in Li_{6}C_{60}H_{2}.

We note that in Li_{6}C_{60}H_{30}, 10 H atoms are bound quasi-molecularly to the Li atoms. The binding energy of these H atoms is clearly less than that for the ones bound in atomic form. To see what this binding energy is, we calculated the energy needed to desorb only the H atoms bound quasi-molecularly using the equation

\[
\langle E_{b}(H_{2}) \rangle = -\frac{[E(Li_{6}C_{60}H_{2}) - E(Li_{6}C_{60}) - 5E(H_{2})]}{5}
\]

This yields a binding energy of 0.14 eV. The corresponding energy when C_{60} contains only one Li atom is 0.17 eV. The substantial reduction in binding energy between H atoms bound quasi-molecularly versus those bound chemically to the C atoms is due to the different mechanisms operative in the bonding scheme. In the former, the bonding is due to a polarization mechanism that is not chemical in nature and hence is weak. We should caution the reader that density functional theory with GGA functional does not include dispersive forces and hence always leads to underbinding. Because DFT within LDA leads to overbinding, it is expected that calculations at the DFT/LDA level of theory may compensate for this omission and may yield a more realistic binding energy when dealing with weak polarization forces. We, therefore, repeated the above calculations using DFT/LDA with the Vosko–Wilk–Nussair (VWN) formula.

The resulting \( \langle E_{b}(H) \rangle \) was found to be 0.28 eV, which is significantly larger than that obtained using the DFT/GGA formalism.

Leaving quantitative comparison aside, we can confidently conclude that there are two types of H atoms bound in Li_{6}C_{60} with very different binding energies. The ones bound more weakly, namely, the quasi-molecular species, will desorb at a lower temperature, while those bound more strongly to the C atom will require elevated temperatures. We should point out that if only the quasi-molecular hydrogen atoms are seen experimentally to reversibly adsorb on Li_{6}C_{60} the gravimetric density should be 1.25 wt % and not 5 wt % as observed. To reconcile this apparent discrepancy, we note that as many as five H_{2} molecules can be bound to a Li atom in free Li_{6}C_{60}.

Because the former binding is much stronger than the latter, we should caution the reader that density functional theory with GGA functional does not include dispersive forces and hence always leads to underbinding. Because DFT within LDA leads to overbinding, it is expected that calculations at the DFT/LDA level of theory may compensate for this omission and may yield a more realistic binding energy when dealing with weak polarization forces. We, therefore, repeated the above calculations using DFT/LDA with the Vosko–Wilk–Nussair (VWN) formula.

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The resulting \( \langle E_{b}(H) \rangle \) was found to be 0.28 eV, which is significantly larger than that obtained using the DFT/GGA formalism.
Zero-point energy correction, on the other hand, reduces the binding energy by about 20%. Because these two omissions compensate for each other, we believe that our conclusions are qualitatively correct. We also note that while these studies are performed on an isolated C_{60} cluster, experiments were carried out in bulk samples where interaction between C_{60} clusters may also be important. However, prior studies showed that the structure of the Li-coated C_{60} remained intact during such interactions, and three H_{2} molecules could still be bound to each Li atom. We are currently carrying out studies of hydrogen storage properties of Li_{x}C_{60} cluster-assembled materials to get a quantitative understanding of hydrogen sorption.

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**Notes**

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