



# Effects of pressure on wetted area of submerged superhydrophobic granular coatings. Part II: poly-dispersed coatings



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## HIGHLIGHTS

- New formulations to characterize performance of superhydrophobic coatings.
- Predictions of wetted area and hydrostatic critical pressure for the coatings.
- Wetted area is important for predicting the water drag force on a surface.
- The proposed method is analytical, easy to use, and relatively accurate.
- Includes poly-dispersed coatings of randomly distributed heterogeneous particles.

## GRAPHICAL ABSTRACT

A simple method is developed to characterize the wettability of superhydrophobic coatings comprised of poly-dispersed particles of different diameters and contact angles by defining mono-dispersed equivalent particle diameters and contact angles for such poly-dispersed coatings.

$$\Delta P_p^{CR} = \Delta P_m^{CR}$$

$$n_1 = n_2 = n_3 = n_4 = 0.25$$

$$\theta_1 = 120^\circ, \theta_2 = 100^\circ, \theta_3 = 80^\circ, \theta_4 = 60^\circ$$

$$d_1 = 72, d_2 = 57, d_3 = 40, d_4 = 31 \mu\text{m}$$

$$\theta_{eq} = \frac{2\pi \cos \theta_i + \sum_{j=1}^k \beta_{j_i} \cos \theta_{j_i}}{k\pi} = 107^\circ$$

$$d_{eq} = \frac{2\pi d_i + \sum_{j=1}^k \beta_{j_i} d_j}{k\pi} = 63 \mu\text{m}$$

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## ABSTRACT

The effects of hydrostatic pressure on the stability of the air–water interface over submerged superhydrophobic coatings comprised of mono-dispersed particles was studied in the first part of this two-part publication [Colloids and Surfaces A, 465 (2015) 87–98]. In this second part, our formulations are extended to cover granular coatings comprised of randomly arranged particles having bi-dispersed or poly-dispersed size and contact angle distributions. Simple analytical formulations are developed to predict how the air–water interface transitions from a non-wetted (Cassie) state to the fully-wetted (Wenzel) state through a series of intermediate wetting states. In particular, a simple mono-dispersed equivalent particle diameter is proposed to be used in predicting the critical pressure and wetted area of poly-dispersed coatings comprised of particles of different diameters and contact angles as a function of hydrostatic pressure. Numerical simulations conducted via the Surface Evolver finite element code have been used to examine the accuracy of the analytical formulations developed in this study.

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## 1. Introduction

The reduced cost of manufacturing has played an important role in making spray-on granular superhydrophobic coatings attractive alternatives to superhydrophobic surfaces produced via microfabrication (see e.g., [1–3]). Such surfaces can be used for applications ranging from self-cleaning and drag reduction to corrosion resistance and heat transfer [4–7]. The essential attribute of superhydrophobic (SHP) surfaces is the reduced water–solid contact area (wetted area), which helps to reduce the friction between a moving body of water and the surface [6–9]. An analytical force

*Abbreviations:* AWI, air–water interface; CCP, critical capillary pressure; CHP, critical hydrostatic pressure; FB, force balance; IA, immersion angle; SVF, solid volume fraction; YLCA, Young–Laplace contact angle; SE, Surface Evolver; ED, equivalent diameter; VED, Voronoi equivalent diameter.

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