

**LARSON—MATH 255—CLASSROOM WORKSHEET 06**  
**Strings, Booleans, and More.**

1. (a) Start the Chrome browser.
- (b) Go to `http://cocalc.com`
- (c) Login using **your VCU email address** .
- (d) Click on our class Project.
- (e) Click “New”, then “Worksheets”, then call it **c06**.
- (f) For each problem number, label it in the Sage cell where the work is. So for Problem 2, the first line of the cell should be `#Problem 2`.

**Lists in Sage**

A *list* is a basic *data structure* in Python and Sage. They are represented by square brackets with comma separated numbers, strings, etc., between them (like `[2, 5, 9]` or `["red", "blue"]`). We have already seen lists in our use of both the `solve()` and `line()` commands which used, respectively, a list of equations and a list of points.

2. Lists can be given names. Evaluate `L=[2,3,5,9]`. Then evaluate `L`.
3. Lists are indexed starting with 0. Evaluate each of `L[0]`, `L[1]`, `L[2]`, and `L[3]`.
4. Lists can be combined with “+”. Evaluate `[2,3,5,9]+[3,4,5]`. (Note: any common elements are repeated.)
5. Let `M=[3,4,5]`. Evaluate `L+M`.
6. If you want all the integers from  $x$  to  $y$  you can use the shorthand notation `[x..y]`. Evaluate `[3..7]`.
7. If you want a list with  $m$   $n$ 's you can use the shorthand notation `[n]*m`. Evaluate `[0]*7`.
8. You can have a list of lists. Evaluate `L=[[0,1],[2,3],[4,5]]`. Now evaluate `L[1]`. Then evaluate `L[1][0]`. What do you think the value of `L[0][1]` is?
9. You can use *list comprehension* to get a list of the values of any function applied to an initial list. Evaluate `[x**2 for x in [2,5,9]]`.
10. Use list comprehension to produce a list of the cubes of all the integers from 2 to 17.
11. List comprehension can also be used to *filter* the numbers in a list. Evaluate `[x for x in [2,5,9] if x%2==0]`. What did this do?
12. Evaluate `[x for x in [2,5,9] if x%2==1]`. What did this do?

**Calculus in Sage**

13. Find the derivatives for  $x^2$ ,  $2x^4$ ,  $\log(x)$ ,  $\sin(x)$ ,  $e^{2x}$ , and  $x^x$  using the command `diff(f(x),x)` (put each function in for `f(x)`).

14. Find the 2<sup>nd</sup> derivatives for  $x^2$ ,  $2x^4$ ,  $\log(x)$ ,  $\sin(x)$ ,  $e^{2x}$ , and  $x^x$  using the command `diff(f(x),x,2)` (put your function in for `f(x)`).
15. Let  $g(x) = x^x$ . Sketch the graph of  $g(x)$ . Let `gprime(x)=diff(g(x),x)`. Evaluate `gprime(1)` and `gprime(0)`. Explain.
16. Sketch the graph of  $gprime(x)$ . Solve when  $gprime(x) = 0$ .
17. Evaluate `derivative(g(x))`. (`diff()` is just shorthand for `derivative()`).
18. Find `g(x).derivative()`.
19. Let  $h(x,y)=xy$ . Find  $\frac{\partial h}{\partial x}$  the partial derivative of  $h(x)$  with respect to  $x$  by hand. Then evaluate  $h(x,y)=xy$ , and `diff(h(x,y),x)`.
20. Let  $h(x,y)=xy$ . Find `diff(h(x,y),x)`.
21. Find  $\frac{\partial h^2}{\partial x \partial y}$ . Now try `diff(h(x,y),x,y)`
22. Find  $\frac{\partial h^2}{\partial x \partial x}$ .
23. Try `h.derivative()`. Explain what you get.
24. Find  $\int 3x dx$  by hand. Check with `integral(3*x,x)`.
25. Let  $f(x)=3x$ . Let `fint=integral(3*x,x)`. Check that `diff(fint,x)=f(x)`.
26. Find  $\int_1^2 f(x) dx$  by hand. Check using `integral(f(x),x,1,2)`.
27. Sketch  $g(t) = t^{20}e^t$  on  $(0, 3)$ .
28. Find  $\int t^{20}e^t dt$ .
29. Find  $\int_2^3 t^{20}e^t dt$ .
30. Find a numerical approximation for  $\int_2^3 t^{20}e^t dt$ .
31. Try `numerical_integral(t20et, 2, 3)`.
32. Find out what the second number of your answer means.

### Getting your classwork recorded

When you are done, before you leave class...

- (a) Click the “Make pdf” (Adobe symbol) icon and make a pdf of this worksheet. (If Cocalc hangs, click the printer icon, then “Open”, then print or make a pdf using your browser).
- (b) Send me an email with an informative header like “Math 255 - c05 worksheet attached” (so that it will be properly recorded).
- (c) Remember to attach today’s classroom worksheet!