

Directions: Closed book, closed notes, no calculators.

1. Find the following derivatives.

$$(a) \frac{d}{dx} [x \ln(x) + \sin^{-1}(x)] = 1 \cdot \ln(x) + x \frac{1}{x} + \frac{1}{\sqrt{1-x^2}}$$

$$= \boxed{\ln(x) + 1 + \frac{1}{\sqrt{1-x^2}}}$$

$$(b) \frac{d}{dx} [(\tan^{-1}(x))^3] = 3(\tan^{-1}(x))^2 \frac{d}{dx} [\tan^{-1}(x)]$$

$$= \boxed{3(\tan^{-1}(x))^2 \cdot \frac{1}{1+x^2}}$$

$$(c) \frac{d}{dx} [4 \ln(3x^3 + 1)] = 4 \frac{1}{3x^3 + 1} \frac{d}{dx} [3x^3 + 1] = 4 \cdot \frac{1}{3x^2 + 1} \cdot 9x^2$$

$$= \boxed{\frac{36x^2}{3x^2 + 1}}$$

2. An object moving on a straight line is  $s(t) = 2 + t + t^3$  feet from its starting point at time  $t$  seconds. Find the object's velocity when its acceleration is 12 feet per second per second.

$$\text{Velocity: } v(t) = s'(t) = 1 + 3t^2$$

$$\text{Acceleration: } a(t) = v'(t) = 6t$$

To find when acceleration is  $12 \text{ ft/sec}^2$ , solve

$$a(t) = 12$$

$$6t = 12$$

$$t = 2$$

Thus acceleration is  $12 \text{ ft/sec}^2$  at time  $t = 2 \text{ sec}$ .

$$\text{Velocity at this time is } v(2) = 1 + 3 \cdot 2^2 = \boxed{13 \text{ ft/sec}}$$