

Name: \_\_\_\_\_

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1. (14 points) An object moving on a straight line is  $s(t) = t^3 - 3t^2$  feet from its starting point at time  $t$ . Find the object's acceleration at the instant its velocity is  $-3$  feet per second.

2. (18 points) This problem concerns the equation  $x^2 = y \cos(y)$ .

(a) Use implicit differentiation to find  $y'$ .

(b) Use part (a) to find the slope of the tangent to the graph of  $x^2 = y \cos(y)$  at the point  $(\sqrt{\pi}, -\pi)$ .

3. (18 points) This problem concerns the function  $f(x) = x^3e^x$

(a) Find the critical points of  $f$ .

(b) State the interval on which  $f$  increases, and on which it decreases.

(c) State the locations ( $x$  coordinates) of any local minima of  $f$ .

(d) State the locations ( $x$  coordinates) of any local maxima of  $f$ .

(e) Identify the locations of any global extrema of  $f(x)$  on the *open* interval  $(-8, -1)$ .