

$$1. \int_1^2 (x^2 + 1) dx = \left[\frac{x^3}{3} + x \right]_1^2 = \left(\frac{2^3}{3} + 2 \right) - \left(\frac{1^3}{3} + 1 \right) = \frac{8}{3} + 2 - \frac{1}{3} - 1$$

$$= \frac{7}{3} + 1 = \frac{7}{3} + \frac{3}{3} = \boxed{\frac{10}{3}}$$

$$2. \int_0^\pi \sin(x) dx = \left[-\cos(x) \right]_0^\pi = -\cos(\pi) - (-\cos(0))$$

$$= -(-1) - (-1) = \boxed{2}$$

3. Find the area under the graph of $y = x^2$ between $x = 0$ and $x = 2$.

$$A = \int_0^2 x^2 dx = \left[\frac{x^3}{3} \right]_0^2 = \frac{2^3}{3} - \frac{0^3}{3} = \boxed{\frac{8}{3} \text{ square units}}$$

4. Find the derivative of the function $F(x) = \int_1^x \frac{1 + \cos(t)}{\sqrt{t+4}} dt$.

By FTC 1,
$$\boxed{F'(x) = \frac{1 + \cos(x)}{\sqrt{x+4}}}$$

5. Find the derivative of the function $y = \int_1^{x^2+x} \frac{1 + \cos(t)}{\sqrt{t+4}} dt$.

This is $y = F(x^2+x)$, where F is the function from #4, above. By the chain rule, $y' = F'(x^2+x)(2x+1)$

$$= \boxed{\frac{1 + \cos(x^2+x)}{\sqrt{x^2+x+4}} (2x+1)}$$

$$1. \int_{-1}^1 (x^2 + 1) dx = \left[\frac{x^3}{3} + x \right]_{-1}^1 = \left(\frac{1^3}{3} + 1 \right) - \left(\frac{(-1)^3}{3} + (-1) \right)$$

$$= \frac{1}{3} + 1 + \frac{1}{3} + 1 = \frac{2}{3} + 2 = \boxed{\frac{8}{3}}$$

$$2. \int_0^1 \sqrt{x} dx = \int_0^1 x^{1/2} dx = \left[\frac{1}{\frac{1}{2}+1} x^{\frac{1}{2}+1} \right]_0^1 = \left[\frac{1}{3/2} x^{3/2} \right]_0^1$$

$$= \left[\frac{2}{3} \sqrt{x^3} \right]_0^1 = \frac{2}{3} \sqrt{1^3} - \frac{2}{3} \sqrt{0^3} = \frac{2}{3} - 0 = \boxed{\frac{2}{3}}$$

3. Find the area under the graph of $y = \sin(x)$ between $x = 0$ and $x = \pi$.

$$A = \int_0^{\pi} \sin(x) dx = \left[-\cos(x) \right]_0^{\pi} = -\cos(\pi) - (-\cos(0))$$

$$= -(-1) - (-1) = \boxed{2 \text{ square units}}$$

4. Find the derivative of the function $F(x) = \int_1^x \frac{\sqrt{t+4}}{1+\cos(t)} dt$.

By FTC 1,
$$\boxed{F'(x) = \frac{\sqrt{x+4}}{1+\cos(x)}}$$

5. Find the derivative of the function $y = \int_1^{\sin(x)} \frac{\sqrt{t+4}}{1+\cos(t)} dt$.

This is $y = F(\sin(x))$ where F is the function from #4, above. By chain rule, $y' = F'(\sin(x)) \cos(x)$

$$= \boxed{\frac{\sqrt{\sin(x)+4}}{1+\cos(\sin(x))} \cos(x)}$$

$$1. \int_0^2 (x^2 + x) dx = \left[\frac{x^3}{3} + \frac{x^2}{2} \right]_0^2 = \left(\frac{2^3}{3} + \frac{2^2}{2} \right) - \left(\frac{0^3}{3} + \frac{0^2}{2} \right)$$

$$= \frac{8}{3} + \frac{4}{2} = \frac{8}{3} + 2 = \frac{8}{3} + \frac{6}{3} = \boxed{\frac{14}{3}}$$

$$2. \int_0^{\pi/4} \sec^2(x) dx = \left[\tan(x) \right]_0^{\pi/4} = \tan(\pi/4) - \tan(0)$$

$$= 1 - 0 = \boxed{1}$$

3. Find the area under the graph of $y = \frac{1}{x}$ between $x = 1$ and $x = e$.

$$A = \int_1^e \frac{1}{x} dx = \left[\ln|x| \right]_1^e = \ln|e| - \ln|1|$$

$$= 1 - 0 = \boxed{1 \text{ square unit}}$$

4. Find the derivative of the function $F(x) = \int_1^x \frac{1+e^t}{\sqrt{t+4}} dt$.

By FTC 1, $\boxed{F'(x) = \frac{1+e^x}{\sqrt{x+4}}}$

5. Find the derivative of the function $y = \int_1^{x^2+x} \frac{1+e^t}{\sqrt{t+4}} dt$.

This is $y = F(x^2+x)$ where F is the function from #4, above. By chain rule, $y' = F'(x^2+x)(2x+1)$

$$= \boxed{\frac{1+e^{x^2+x}}{\sqrt{x^2+x+4}}(2x+1)}$$

$$1. \int_{-1}^1 (x^3 + 1) dx = \left[\frac{x^4}{4} + x \right]_{-1}^1 = \left(\frac{1^4}{4} + 1 \right) - \left(\frac{(-1)^4}{4} + (-1) \right) \\ = \frac{1}{4} + 1 - \frac{1}{4} + 1 = \boxed{2}$$

$$2. \int_0^\pi \cos(x) dx = \left[\sin(x) \right]_0^\pi = \sin(\pi) - \sin(0) = 0 - 0 = \boxed{0}$$

3. Find the area under the graph of $y = e^x$ between $x = 0$ and $x = 1$.

$$A = \int_0^1 e^x dx = \left[e^x \right]_0^1 = e^1 - e^0 = \boxed{e-1 \text{ square units}}$$

4. Find the derivative of the function $F(x) = \int_1^x \frac{\cos(t+2)}{t^3+1} dt$.

By FTC 1,
$$\boxed{F'(x) = \frac{\cos(x+2)}{x^3+1}}$$

5. Find the derivative of the function $y = \int_1^{x^2+1} \frac{\cos(t+2)}{t^3+1} dt$.

This is $y = F(x^2+1)$ where $F(x)$ is the function from #4 above. By chain rule, $y' = F'(x^2+1)(2x+0)$

$$\frac{\cos(x^2+1+2)}{(x^2+1)^3+1} 2x = \boxed{\frac{\cos(x^2+3)}{(x^2+1)^3+1} 2x}$$