

Name: Richard

MATH 200 - QUIZ 13

Instructions: Show work and put a box around your final answer.

April 18, 2013

1.
$$\sum_{k=1}^5 (3+2k) = (3+2 \cdot 1) + (3+2 \cdot 2) + (3+2 \cdot 3) + (3+2 \cdot 4) + (3+2 \cdot 5)$$
$$= 3 + 2 + 3 + 4 + 3 + 6 + 3 + 8 + 3 + 10$$
$$= 5 \cdot 3 + 2 + 4 + 6 + 8 + 10$$
$$= 15 + 30 = \boxed{45}$$

2. Suppose that $f(x)$ is a function for which $\int_1^5 f(x) dx = 3$ and $\int_1^7 f(x) dx = -6$. Find $\int_5^7 f(x) dx$.

By definite integral property:
$$\int_1^7 f(x) dx = \int_1^5 f(x) dx + \int_5^7 f(x) dx$$
$$-6 = 3 + \int_5^7 f(x) dx$$

Therefore:
$$\int_5^7 f(x) dx = \boxed{-9}$$

3. Write the integral that finds area under the curve $y = \sin^2(x)$ from $x = 0$ to $x = \pi$.

Do not compute the integral.

$$\int_0^{\pi} \sin^2(x) dx$$

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1.
$$\sum_{k=1}^4 (8-2k) = (8-2 \cdot 1) + (8-2 \cdot 2) + (8-2 \cdot 3) + (8-2 \cdot 4)$$
$$= 8 - 2 + 8 - 4 + 8 - 6 + 8 - 8$$
$$= 6 + 4 + 2 + 0 = \boxed{12}$$

2. Suppose that $f(x)$ is a function for which $\int_2^5 f(x) dx = 4$ and $\int_2^8 f(x) dx = 9$. Find $\int_5^8 f(x) dx$.

Definite integral property:
$$\int_2^8 f(x) dx = \int_2^5 f(x) dx + \int_5^8 f(x) dx$$
$$9 = 4 + \int_5^8 f(x) dx$$

Therefore
$$\int_5^8 f(x) dx = \boxed{5}$$

3. Write the definite integral that finds area under the curve $y = e^x + 2x$ from $x = 1$ to $x = 4$.

Do not compute the integral.

$$\int_1^4 (e^x + 2x) dx$$

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$$\begin{aligned} 1. \sum_{k=1}^4 (2k-4) &= (2 \cdot 1 - 4) + (2 \cdot 2 - 4) + (2 \cdot 3 - 4) + (2 \cdot 4 - 4) \\ &= 2 - 4 + 4 - 4 + 6 - 4 + 8 - 4 \\ &= -2 + 0 + 2 + 4 = \boxed{4} \end{aligned}$$

2. Suppose that $f(x)$ is a function for which $\int_2^5 f(x) dx = 7$ and $\int_2^8 f(x) dx = 8$. Find $\int_5^8 f(x) dx$.

Definite integral property: $\int_2^8 f(x) dx = \int_2^5 f(x) dx + \int_5^8 f(x) dx$

$$8 = 7 + \int_5^8 f(x) dx$$

Therefore $\int_5^8 f(x) dx = 8 - 7 = 1$

3. Write the definite integral that finds area under the curve $y = \sqrt{\sin(x)}$ from $x = 0$ to $x = \pi$. Do not compute the integral.

$$\int_0^{\pi} \sqrt{\sin(x)} dx$$

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$$\begin{aligned} 1. \sum_{k=1}^4 (k^2 + 2) &= (1^2 + 2) + (2^2 + 2) + (3^2 + 2) + (4^2 + 2) \\ &= 3 + 6 + 11 + 18 = \boxed{38} \end{aligned}$$

2. Suppose that $f(x)$ is a function for which $\int_0^5 f(x) dx = -7$ and $\int_0^6 f(x) dx = 9$. Find $\int_5^6 f(x) dx$.

Definite integral property: $\int_0^6 f(x) dx = \int_0^5 f(x) dx + \int_5^6 f(x) dx$

$$9 = -7 + \int_5^6 f(x) dx$$

Thus $\int_5^6 f(x) dx = 9 + 7 = 16$

3. Write the definite integral that finds area under the curve $y = 2e^{\cos x}$ from $x = 1$ to $x = 4$. Do not compute the integral.

$$\int_1^4 2e^{\cos(x)} dx$$