

Name: Richard

MATH 200 - QUIZ 12 \$

Instructions: Show work and put a box around your final answer.

April 11, 2013

$$1. \lim_{x \rightarrow 0} \frac{e^{\sin x} - 1}{x} = \lim_{x \rightarrow 0} \frac{e^{\sin(x)} \cos(x)}{1} = e^{\sin(0)} \cos(0) = e^0 \cdot 1 = \boxed{1}$$

↑
form $\frac{0}{0}$

↑
L'Hôpital's Rule

$$2. \int \left(4x + \frac{1}{x} + \sin(x) \right) dx = 4 \frac{1}{2} x^2 + \ln|x| - \cos(x) + C = \boxed{2x^2 + \ln|x| - \cos(x) + C}$$

$$3. \int e^{3x} dx = \boxed{\frac{1}{3} e^{3x} + C}$$

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$$1. \lim_{x \rightarrow \frac{\pi}{2}} \frac{\cos(x)}{\sin(2x)} = \lim_{x \rightarrow \frac{\pi}{2}} \frac{-\sin(x)}{2 \cos(2x)} = \frac{-\sin(\pi/2)}{2 \cos(2 \cdot \pi/2)} = \frac{-\sin(\pi/2)}{2 \cos(\pi)} = \frac{-1}{2 \cdot (-1)} = \boxed{\frac{1}{2}}$$

↑
form $\frac{0}{0}$

↑
L'Hôpital's Rule

$$2. \int (e^x + e + \sec^2(x)) dx = \boxed{e^x + ex + \tan(x) + C}$$

$$3. \int \frac{2}{|x|\sqrt{x^2-1}} dx = 2 \int \frac{1}{|x|\sqrt{x^2-1}} dx = \boxed{2 \sec^{-1}(x) + C}$$

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$$1. \lim_{x \rightarrow 0} \frac{3x}{1 - e^{\sin x}} = \lim_{x \rightarrow 0} \frac{3}{0 - e^{\sin(x)} \cos(x)} = \frac{3}{-e^0 \cos(0)} = \frac{3}{-1 \cdot 1} = \boxed{-3}$$

↑
form $\frac{0}{0}$

↑
L'Hôpital's Rule

$$2. \int (2e^x + x^4 + \sec(x) \tan(x)) dx = \boxed{2e^x + \frac{1}{5}x^5 + \sec(x) + C}$$

$$3. \int \frac{5}{\sqrt{1-x^2}} dx = \boxed{5 \sin^{-1}(x) + C}$$

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$$1. \lim_{x \rightarrow \frac{\pi}{2}} \frac{2x - \pi}{\cos(2\pi - x)} = \lim_{x \rightarrow \frac{\pi}{2}} \frac{2 - 0}{-\sin(2\pi - x)(-1)} = \frac{2}{-\sin(\frac{3\pi}{2})(-1)} = \frac{2}{\sin(\frac{3\pi}{2})} = \frac{2}{-1} = \boxed{-2}$$

↑
form $\frac{0}{0}$

↑
L'Hôpital's Rule

$$2. \int (\sqrt[3]{x} + \cos(x)) dx = \int (x^{\frac{1}{3}} + \cos(x)) dx = \frac{1}{\frac{1}{3}+1} x^{\frac{1}{3}+1} + \sin(x) + C$$
$$= \frac{1}{\frac{4}{3}} x^{\frac{4}{3}} + \sin(x) + C = \frac{3}{4} x^{\frac{4}{3}} + \sin(x) + C$$

$$3. \int \frac{2}{1+x^2} dx = 2 \int \frac{1}{1+x^2} dx =$$

$$\boxed{2 \tan^{-1}(x) + C}$$

$$= \boxed{\frac{3}{4} \sqrt[3]{x^4} + \sin(x) + C}$$