

The Propositional Calculus (Summary)

Symbols

Atom particles:	P Q R	
Atom suffix:	'	(prime)
Prefix operation:	~	(not)
Infix operations:	^ v ⊃	(and, or, if-then/implies)
Infix op boundaries:	< >	(begin op, end op)
Fantasy boundaries:	[]	(push, pop)

Rules of Formation

RULE #0: All atoms are well-formed	atoms
RULE #1: If x is well-formed, then so is $\sim x$	$\sim x$
RULE #2: If x and y are well-formed, then so is $\langle x \wedge y \rangle$	$\langle x \wedge y \rangle$
RULE #3: If x and y are well-formed, then so is $\langle x \vee y \rangle$	$\langle x \vee y \rangle$
RULE #4: If x and y are well-formed, then so is $\langle x \supset y \rangle$	$\langle x \supset y \rangle$

Axioms

None

Rules of Inference

Rule	Prior Theorem	Consequent Theorem
JOINING RULE	x and y	$\langle x \wedge y \rangle$
SEPARATION RULE	$\langle x \wedge y \rangle$	x and y
DETACHMENT RULE	x and $\langle x \supset y \rangle$	y
CONTRAPOSITIVE RULE	$\langle x \supset y \rangle$ $\langle \sim y \supset \sim x \rangle$	$\langle \sim y \supset \sim x \rangle$ $\langle x \supset y \rangle$
DE MORGAN'S RULE	$\langle \sim x \wedge \sim y \rangle$ $\sim \langle x \vee y \rangle$	$\sim \langle x \vee y \rangle$ $\langle \sim x \wedge \sim y \rangle$
SWITCHEROO RULE	$\langle x \vee y \rangle$ $\langle \sim x \supset y \rangle$	$\langle \sim x \supset y \rangle$ $\langle x \vee y \rangle$
DOUBLE-TILDE RULE ^a	Any string with $\sim\sim$ Any string	Same string with one less $\sim\sim$ Same string with one more $\sim\sim$
FANTASY RULE	If y can be derived given x	$\langle x \supset y \rangle$

^aValid only if resulting string is well-formed